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***Ab initio* study of the CO–N₂ complex: A new highly accurate intermolecular potential energy surface and rovibrational spectrum**

Hubert Cybulski*

*Institute of Physics, Faculty of Physics, Astronomy and Informatics,
Nicolaus Copernicus University in Torun,
Grudziadzka 5, 87-100 Torun, Poland*

Christian Henriksen†

*Department of Applied Mathematics and Computer Science,
Technical University of Denmark,
2800 Kgs. Lyngby, Denmark*

Richard Dawes‡

Missouri University of Science and Technology, Rolla, MO 65409, USA

Xiao-Gang Wang§, Neha Bora, Gustavo Avila, and Tucker Carrington Jr.¶

*Chemistry Department, Queen's University,
Kingston, Ontario K7L 3N6, Canada*

Berta Fernández**

*Department of Physical Chemistry, University of Santiago de Compostela
15782 Santiago de Compostela, Spain*

* Electronic mail: hubert@fizyka.umk.pl, hcybulski@gmail.com

† Electronic mail: chrh@dtu.dk

‡ Electronic mail: dawesr@mst.edu

§ Electronic mail: xgwang.dalian@gmail.com

¶ Electronic mail: tucker.carrington@queensu.ca, Fax: 613-533-6669

** Electronic mail: berta.fernandez@usc.es

Abstract

A new, highly accurate *ab initio* ground-state intermolecular potential-energy surface (IPES) for the CO-N₂ complex is presented. Thousands of interaction energies calculated with the CCSD(T) method and Dunning’s aug-cc-pVQZ basis set extended with midbond functions were fitted to an analytical function. The global minimum of the potential corresponds to the geometry characterized by $r_0 = 7.856 a_0$, $\theta_1 = 111.3^\circ$, $\theta_2 = 159.7^\circ$, and $\phi_2 = 0^\circ$ and has an energy of -118.2 cm^{-1} . The symmetry-adapted Lanczos algorithm was used to compute rovibrational energies (up to $J = 20$) on the new IPES. The RMSE with respect to experiment was found to be on the order of 0.038 cm^{-1} which confirms the very high accuracy of the potential. This level of agreement is among the best reported in the literature for weakly bound systems and considerably improves on those of previously published potentials.

I. INTRODUCTION

From the theoretical point of view accurate studies of weakly bound complexes pose a challenge. Not only are sophisticated methods accounting for electron-correlation effects required, but also extended basis sets are essential in order to obtain the results that, on one hand, can be compared with highly accurate experimental data and, on the other, can be used to make predictions in cases where good quality experimental data are not available. Furthermore, to obtain reliable intermolecular potential energy surfaces (IPESs) for complexes with more than 2 intermolecular coordinates the evaluation of thousands of *ab initio* interaction energies is inevitable. To compute an accurate spectrum one must, after obtaining the IPES, solve the ro-vibrational Schroedinger without making approximations.

The CO-N₂ dimer is a simple van der Waals (vdW) complex in which the intermolecular forces between two isoelectronic molecules, carbon monoxide (barely polar) and nitrogen (nonpolar), are of significant interest from the experimental and theoretical points of view. This system is of great relevance in atmospheric chemistry since N₂ is one of the primary atmospheric constituents and CO is an important gaseous pollutant. Precise measurements and theoretical predictions of the effects of pressure and temperature on the spectrum of CO perturbed by the dominant atmospheric species, N₂ and O₂, are indispensable for the interpretation of atmospheric absorption data.

Spectra of the CO-N₂ complex were first reported in 1996, when infrared (IR) spectra in the region of the CO fundamental band (2146 cm⁻¹) were recorded by Kawashima and Nishizawa [1] and by Xu and McKellar [2]. In their experimental work Xu and McKellar [2] recorded the slit-jet IR spectrum of the complex in the 4.7 μm region of the CO stretching vibration. They obtained a very simple spectrum, that could be interpreted as that of a (fictitious) system formed by a CO molecule and a rare gas atom of a mass of 28 a.m.u., due to an almost free rotation of the N₂ molecule in the complex. An effective intermolecular separation of 4.025 Å was deduced. Unfortunately, the results did not provide information about the angular orientation of the N₂ molecule within the complex. The authors pointed out the need for theoretical calculations in order to predict the energy levels for higher lying excited states.

Pure rotational spectra of CO-N₂ with the ¹⁴N and ¹⁵N isotopes were observed by Kawashima *et al.* [3]. The authors also showed that, regarding the orientation of the N₂

subunit and van der Waals stretching force constant, the CO-N₂ dimer is similar to the Ar-N₂ and Kr-N₂ complexes.

At the same time, Xu *et al.* [4] studied the microwave and millimeter wave transitions of the *ortho*N₂ states of the complex. Nuclear quadrupole hyperfine splittings were resolved and analysed in order to acquire additional information on the angular anisotropy of the IPES and the rotational and ro-vibrational spectra of two additional (¹³C and ¹⁸O) isotopomers were measured, too. The authors confirmed a planar, approximately T-shaped structure for the ground state of the complex ($K = 0$), with N₂ as the top, CO as the leg, and with the O atom on average closer to N₂ than the C atom.

In a complementary investigation [5] the rotational and ro-vibrational spectra of the CO-*para*N₂ complex were measured using a microwave spectrometer in the frequency region from 4 to 26 GHz. The behaviour of the complex could be interpreted neither in terms of a semirigid rotor model nor in terms of a totally free internal rotor. Therefore, the authors used several semirigid geometries associated with different K values. They confirmed, as in Ref. 4, a similar planar, approximately T-shaped structure for the ground state ($K = 0$) of the *ortho*N₂ state of the complex with an intermolecular distance of 4.026 Å calculated from the experimental rotational constants using a pseudodiatom approximation. The authors pointed out that N₂ undergoes an almost free internal rotation within the complex. The geometry in the *ortho*N₂ lower $K = 1$ state is also T-shaped with N₂ forming the leg and CO the top. The two investigated *para*N₂ $K = 1$ states correspond to the N₂ molecule in a more nearly perpendicular orientation with respect to the intermolecular axis, whereas in the $K = 0$ stack of the first excited bending state the N₂ is located parallel to this axis. The values of the intermolecular distances were also reported for these states.

The IR spectrum of CO-N₂ was further studied using a pulsed supersonic slit-jet and a rapid-scan tunable diode laser [6]. In the case of the CO-*para*N₂ spin modification, the previous tentative assignment of just one subband [1, 2] was extended to include over 10 linked subbands in terms of three ground ($v_{\text{CO}} = 0$) state stacks of levels (with $K = 0$ and 1), and 7 excited state ($v_{\text{CO}} = 1$) stacks (with $K = 0, 1$ and 2). In the case of the more abundant form, CO-*ortho*N₂, an excited bending state was observed for the first time for both $v_{\text{CO}} = 0$ and 1.

The first observation of the bending vibration of the CO-N₂ complex in the millimeter wave range from 130 to 155 GHz was reported in Ref. 7, providing precise information

about the vibrational frequency and the rotational constants for this state. Six transitions, $P(2)$, $P(1)$, $R(0)$, $R(1)$, $R(2)$, and $R(3)$, associated with the ground and bending state $K = 0$ levels of the *ortho*N₂ spin modification, were measured and analysed.

In 2006, Surin *et al.* [8] carried out new measurements of the CO-N₂ rotational transitions, and in 2015 the studies were completed by reporting new millimeter-wave transitions [9]. The authors concluded that in the $K = 0$ state CO-*para*N₂ has a geometry similar to that in the lower $K = 1$ state of CO-*ortho*N₂, with N₂ as the leg and CO as the top of the T-shaped complex, while in the $K = 2$ state N₂ forms the top and CO – the leg. The authors pointed out the necessity of theoretical research as an essential tool in the interpretation of the already available highly accurate experimental data.

In a recent paper [10], an analysis of a new broad-band (2135–2165 cm⁻¹) spectrum of CO-N₂ obtained using a tunable continuous-wave quantum-cascade laser and a pulsed supersonic slit-jet source was presented. Almost 100 new rovibrational levels were assigned to nine new stacks, of which four are in the excited state of CO-*ortho*N₂, three in the excited state of CO-*para*N₂, and two in the ground state ($\nu_{\text{CO}} = 0$) of CO-*para*N₂. The calculated rotational constants for the various rotational level stacks varied from 0.0638 to 0.0768 cm⁻¹ which corresponds to a range of 4.34 to 3.96 Å for the effective intermolecular center-of-mass distance. However, using these data the authors could not resolve the CO-N₂ structure unambiguously and concluded that dynamical calculations of rotational energy levels are necessary.

The most important theoretical studies on the complex are the most recent. Fišer and Polák [11] investigated 11 structures of the complex using the coupled-cluster singles and doubles including connected triple corrections [CCSD(T)] and Møller-Plesset perturbation theory up to fourth order (MP4) methods and Dunning’s correlation consistent augmented polarized valence aug-cc-pVXZ (X= D, T, Q) bases extended with a set of *3s3p2d1f1g* midbond functions. These results were further complemented with some new data [12]. The authors concluded that the results of the calculations support a considerable non-rigidity of the complex and the presence of multiple, nearly equally deep minima on the IPES, separated by barriers of about 1 cm⁻¹ height. The most stable structures were two distorted T-shaped configurations where the N-atom is pointing towards the C-O bond, with intermolecular distances of ca. 4.1 Å and CCSD(T)/aug-cc-pVQZ+*3s3p2d1f1g* interaction energies of -118.2 and -117.4 cm⁻¹. The interaction energy value for the first configuration

was already close to the estimated complete basis-set (CBS) limit of 118.5 cm^{-1} [12].

The *ab initio* study of the $(\text{N}_2)_n\text{CO}_m$ ($n = 1-7$; $m = 1-3$) complexes at the MP2 and CCSD(T) levels of theory with the 6-311+G* basis set showed that the CO-N₂ dimer exists in the form of a series of structurally different but energetically almost equivalent isomers [13]. According to the calculations, the interconversion between the conformers proceeds with the barriers not exceeding $0.07\text{ kcal mol}^{-1}$. Therefore, the internal movement of the molecules in the CO-N₂ system is practically free.

The first *ab initio* IPES obtained for CO-N₂ was published by Karimi-Jafari *et al.* [14] in 2011. The authors calculated a four-dimensional potential employing the MP4 method with a basis set obtained from the aug-cc-pVQZ basis set of Dunning and coworkers [15] by removing all the *g* and *f* functions; this basis was further supplemented by a set of *3s3p2d1f* midbond functions [16, 17]. In contrast to previous experimental results the authors found that the intermolecular potential is characterized by a single, distorted T-shaped minimum (and its symmetrically equivalent partners) with CO at the top and N₂ on the leg of the T, and an energy of -123.1 cm^{-1} . This structure is similar to that assigned to an excited state in Ref. 5. The T-shaped ground state structure reported in Ref. 5 is identified on the MP4 IPES as a saddle point [14]. In order to estimate the correlation method error, the authors compared their MP4 interaction energies with the CCSD(T) energies calculated with Dunning’s aug-cc-pVTZ basis set augmented with the *3s3p2d1f* set of midbond functions. The differences were about 5 cm^{-1} in the proximity of the global minimum but rose to 15 cm^{-1} for the linear orientations of the complex.

The CO-N₂ complex still remains a very attractive object for both theoretical and experimental studies and only very recently two papers [18, 19] concerning this system have been published.

Liu *et al.* [18] generated a five-dimensional IPES which accounted for the stretching of the C-O bond. The IPES was calculated with the explicitly correlated CCSD(T)-F12b method and the aug-cc-pVQZ basis set. A global minimum with a well depth of -117.417 cm^{-1} was found at $\theta_1 = 73.0^\circ$, $\theta_2 = 13.8^\circ$, $\phi = 0.0^\circ$, $R = 4.155\text{ \AA}$, corresponding to a distorted T-shaped structure with N₂ pointing towards the C-O bond. The authors reported RMSE discrepancies with respect to experimental data smaller than 0.068 cm^{-1} in the predicted IR transitions and intensities for the CO-*ortho*N₂ complex as well as in the calculated energy levels for CO-*para*N₂. Nonetheless, a considerable number of the misprints in the table with

the energy levels makes this statement difficult to confirm.

The second *ab initio* calculated four-dimensional IPES has been reported by Surin *et al.* [19]. The calculations were carried out using the CCSD(T) method and the aug-cc-pVQZ basis set supplemented with midbond functions. The found global minimum of the IPES corresponds to the structure of $\theta_{\text{CO}} = 109.4^\circ$, $\theta_{\text{N}_2} = 162.8^\circ$, and $\varphi = 0^\circ$ and $R_e = 7.86 a_0$, and has an energy of -117.35 cm^{-1} . Also a new millimeter-wave survey for the CO-N₂ complex in the frequency range of 110–145 GHz was performed and several transitions not previously observed were detected and assigned. The computed energy levels were compared with the available experimental data and the authors found good agreement with experiment for all detected stacks. However, they noted that a significant number of the detected lines could still not be assigned.

However, it seems that each of the three published potentials suffers from some limitations. The potential for CO-N₂ from Ref. 14 is the least reliable. First, the MP4 method is well-known for overestimating interaction energies. Second, the authors removed from the basis set a significant portion of the diffuse functions that are responsible for a correct description of the intermolecular interactions. Third, the number of grid points that the authors used in their calculations does not seem to be sufficient to properly reproduce the anisotropy of the interaction, especially in the regions of short intermolecular distances.

The explicitly correlated CCSD(T)-F12 method [20–23], used in the calculations of the second potential [18], is becoming quite popular since contributions to calculated molecular correlation energies coming from single and double excitations are well converged with relatively small orbital bases. However, it seems that in the case of weak intermolecular interactions the errors introduced by the a/b/* approximations in CCSD-F12 and by a non-explicitly correlated treatment of perturbative triples (with or without scaling) can become crucial at this level of accuracy [24]. It was also shown that, on one hand, CCSD(T)-F12 methods tend to perform more poorly for larger basis sets, but on the other, addition of midbond sets significantly improves the F12 calculated interaction energies. The authors in Ref. 18 did not test convergence of their method neither using larger bases or employing midbond functions.

The third potential [19] was obtained using the conventional CCSD(T) method and the aug-cc-pVQZ basis set further extended with a set of *3s2p1d* midbond functions; however, remarkable discrepancies between the calculated and experimental rotational states were

still observed.

In this work we present a new four-dimensional interaction potential that seems to overcome all the above-mentioned deficiencies. The interaction energies were calculated at the CCSD(T) level, with the aug-cc-pVQZ basis set further extended with a set of $3s3p2d1f1g$ midbond functions. For several representative geometries of the system we confirmed that the employed number of grid points is sufficient to correctly reproduce the anisotropy of the potential. Next, the calculated *ab initio* interaction energies were fitted to an analytic expression. Then, the IPES was employed in calculations of the intermolecular states. The agreement between the calculated and experimental states is remarkably better than that reported for both of the most recent potentials [18, 19].

The manuscript is organized as follows: In Sec. II the details of the quantum-chemical calculations are given, then, in Sec. II B the results of the basis set studies are presented. In Sec. III we describe the analytical fit of the obtained IPES and some of its features, and in Sec. IV the details of the intermolecular-states studies are reported. Finally, in Sec. V we summarize and conclude.

II. QUANTUM-CHEMICAL CALCULATIONS OF THE IPES

A. Computational details

The coordinates describing the geometries used in the calculations are as follows. r_0 is the intermolecular distance between the centers of mass of the monomers, θ_1 and θ_2 are the angles between each of the molecular axis (1 for CO and 2 for N₂) and the intermolecular axis, and ϕ_2 is the difference between the azimuthal angles. For θ_2 set to 180.0° (or 0.0°) the values of $\theta_1 = 0.0$ and 180.0° correspond to the linear CO \cdots N₂ and OC \cdots N₂ geometries, respectively. In all calculations we fix the CO and N₂ interatomic distances to the experimental 1.128323 Å and 1.09768 Å values [25], respectively. The intermolecular coordinates are depicted in Fig. 1.

Due to the good performance of the methodology employed in our previous studies on accurate calculation of IPESs of other vdW systems (Refs. 26, 27 and references cited therein), the interaction energies are corrected for the basis set superposition error (BSSE) using the counterpoise method [28] and are evaluated at the CCSD(T) level with the MOLPRO program [29]. In basis set completeness studies, we employed Dunning’s doubly augmented

correlation consistent basis sets, i.e. x-aug-cc-pVXZ (x= -, d; X= D, T, Q, 5; in the following denoted as xaXZ), as well as the core-valence aug-cc-pCVXZ (X= T, Q; denoted here as aCXZ) basis sets. These bases were extended with a set of $3s3p2d1f1g$ midbond functions (denoted as 33211) with exponents of 0.90, 0.30, and 0.10 for the s and the p functions, 0.60 and 0.20 for the d functions, and 0.30 for the f and g functions, that are placed in the middle of the van der Waals bond [30–32]. Relativistic effects were assessed using the second order Douglas-Kroll-Hess Hamiltonian as implemented within the MOLPRO program [29]

B. Basis set study

The results of the basis set study are presented in Tab. I. We chose 13 geometries with $r_0 = 4.4980 \text{ \AA}$ ($8.5 a_0$), $\theta_1 = \theta_2$, and $\phi_2 = 0.0^\circ$. This slice cuts the IPES in the proximity of the global minimum of the system and allow us to compare the results with those reported in Ref. 14.

The overall shape of the potential slices is in qualitative agreement with that drawn in Fig. 1 of Ref. 14. As expected, the interaction energy increases (in absolute value) going from the aDZ to a5Z basis set. The convergence is faster with addition of midbond functions to the bases. However, the aQZ+33211 slice is slightly shallower than the aTZ+33211 one (by ca. 0.8 cm^{-1} for the lowest energy). This probably results from the fact that the slice does not pass directly through the global minimum and the topography of the IPES changes somewhat with basis set size. We further tested the influence of the frozen core approximation on the calculated interaction energies employing the core-valence aCXZ basis sets as well as the fully uncontracted ones. This effect is noticeable, but if we compare the results obtained within the frozen-core approximation with aQZ+33211 and those where all electrons were correlated with the aCQZ+33211 basis set for the geometry corresponding to the lowest interaction energy, the difference does not exceed 0.1 cm^{-1} (see Tab. I).

Further tests showed (*cf.* Tab. I) that relativistic effects are negligible (significantly smaller than 0.01 cm^{-1} in the region of the global minimum) in the case of the CO-N₂ complex.

Since an appropriate choice of basis set balances the corresponding accuracy and the total cost, given the required number of geometries, we decided to carry out the calculations for the whole surface at the frozen core CCSD(T) level with the aQZ basis set augmented with

the 33211 set of midbond functions.

C. Choice of the number of grid points

To choose correctly the number of grid points we perform some test calculations for different orientations of CO-N₂. Representative results for a region characterized by a pronounced anisotropy, are depicted in Fig 2. The coordinates of the chosen geometries are $r_0 = 3.70426 \text{ \AA}$ ($7.0 a_0$), $\theta_1 = 90^\circ$, and $\phi_2 = 0.0^\circ$, and the values of θ_2 correspond to the abscissas of n -points Gauss-Lobatto quadrature. Here, we use the Gauss-Lobatto points since they include also points corresponding to 0 and 180 degrees unlike the Gauss-Legendre points employed in Ref. 14. The Gauss-Lobatto point distribution is similar to the distribution of the Legendre points used to compute the spectrum (see Sec. IV A). This ensures that the IPES is accurate where it is evaluated. The interaction energies are interpolated using $n = 10, \dots, 16$ nodes. The *ab initio* calculated interaction energy values (black circles) employed in all the interpolations as well as some additionally calculated energies (red circles) are also presented in Fig 2. It is clear that the interpolated curves yield the correct overall shape of the exact curve and the accuracy increases with an increase of n . The exceptions are the regions where θ_2 approaches 0 or 180 degrees, namely, in the proximities of the two T-shape geometries. The performance of the interpolations is worse for all the cases with an even n , mainly because they do not behave correctly at $\theta_2 = 0$ and 180 (*cf.* Fig 2a and b). For the 10-point Gauss-Lobatto grid the differences between the interpolated and exact *ab initio* values exceed 2 cm^{-1} . The interpolations based on an odd number of points converge towards the correct shape of the curve; however, for this highly anisotropic orientation of the system such a convergence is slow. For other orientations of CO-N₂ of lower anisotropy (not shown here) their performance is much more satisfactory.

Taking into account the above considerations, in the calculations of the IPES we decided to employ the 13-points Gauss-Lobatto grid for θ_1 and θ_2 . This choice seems to be the optimal compromise between the desired accuracy and reliability and available computational resources. In most calculations we consider 12 intermolecular distances in a_0 : 5.0, 6.0, 7.0, 8.0, 9.0, 10.0, 11.0, 12.0, 14.0, 18.0, 23.0, 30.0. For some orientations we make additional calculations for distances of 4.0 and 40.0 a_0 . The values of ϕ_2 correspond to the abscissas of 9-points Gauss-Lobatto quadrature. Because of the symmetry of the system θ_1 and θ_2 are

varied between 0 and 180 degrees (13 grid points for each angle), while ϕ_2 between 0 and 90 degrees (only 5 points are needed to be calculated for this angle). In total, the calculations are performed for slightly more than 10 100 different geometries of the dimer.

III. FITTING OF THE IPES

Having determined the interaction energies for specific geometries *via ab initio* methods, we now turn to constructing an analytical model of the IPES. The analytical expression will be useful in other applications where a compact form of a potential is indispensable. Here, we model the IPES as a many body expansion, that is, as a function of the distances between the atoms in the complex.

The complex consists of two molecules CO and N₂, the latter of which we consider made up of two atoms N and N'. Given a configuration of the complex, we can compute the following four distances

$$d_1 = d(C, N) \tag{1}$$

$$d_2 = d(C, N') \tag{2}$$

$$d_3 = d(O, N) \tag{3}$$

$$d_4 = d(O, N') \tag{4}$$

Define the dimensionless quantities, D_i , by

$$D_i = \exp(-ad_i/d_{\text{ref}}), \quad i = 1, 2, 3, 4, \tag{5}$$

where the constant $d_{\text{ref}} = 8a_0$ is chosen to be the approximate distance between the two molecules, and the dimensionless constant a , the dilatation, is an adjustable parameter to be determined.

With four exponents (e_1, e_2, e_3, e_4) , we define the symmetrized term

$$T_{(e_1, e_2, e_3, e_4)} = \frac{1}{2} (D_1^{e_1} D_2^{e_2} D_3^{e_3} D_4^{e_4} + D_1^{e_2} D_2^{e_1} D_3^{e_4} D_4^{e_3}). \tag{6}$$

Notice that if we exchange the positions of N and N' (which does not change the shape of the complex), we interchange the value of d_1 and d_2 as well as that of d_3 and d_4 . However, the value of the symmetrized term does not change.

Our model of the interaction surface V is a linear combination of symmetrized terms [26, 33, 34], so that

$$V = \sum_{\mathbf{e} \in E} c_{\mathbf{e}} T_{\mathbf{e}} \quad (7)$$

where E is the set of selected exponents, and we have written $\mathbf{e} = (e_1, e_2, e_3, e_4)$. So if we, for example, suppose that $E = \{(1, 0, 0, 0), (2, 1, 0, 1)\}$, we obtain

$$V = c_{1000} T_{(1,0,0,0)} + c_{2101} T_{(2,1,0,1)}, \quad (8)$$

where we write e.g. c_{1000} as a short hand for $c_{(1,0,0,0)}$. Now

$$T_{(1,0,0,0)} = \frac{1}{2} (D_1^1 D_2^0 D_3^0 D_4^0 + D_1^0 D_2^1 D_3^0 D_4^0) = \frac{1}{2} (D_1 + D_2) \quad (9)$$

and

$$T_{(2,1,0,1)} = \frac{1}{2} (D_1^2 D_2^1 D_3^0 D_4^1 + D_1^1 D_2^2 D_3^1 D_4^0) = \frac{1}{2} (D_1^2 D_2 D_4 + D_1 D_2^2 D_3). \quad (10)$$

Thus

$$V = \frac{c_{1000}}{2} (D_1^2 D_2 D_4 + D_1 D_2^2 D_3) + \frac{c_{2101}}{2} (D_1^2 D_2 D_4 + D_1 D_2^2 D_3). \quad (11)$$

We pick 79 different symmetrized terms which gives us 80 adjustable parameters: the dilatation parameter a on which the fitting function depends in a non-linear way, and the 79 coefficients, $c_{\mathbf{e}}$, defining the linear combination (i.e for fixed a , V depends linearly on the last 79 parameters). Because we do not include the term with exponents $(0, 0, 0, 0)$, the IPES will necessarily tend to zero when the distances tend towards infinity. We determined which symmetrized terms to use by heuristically searching for the set of 79 terms giving the best fit among all terms of degree less than or equal to 6.

After determining the fit, we modified V for small distances. This is to avoid physically unreasonable behavior when two atoms are close to each other, such as wildly oscillating interaction energies, or deeply negative energies. More precisely, we set

$$V_{\text{mod}} = E_{\text{big}} \exp(-k d_1 d_2 d_3 d_4) + V(1 - \exp(-k d_1 d_2 d_3 d_4)), \quad (12)$$

where k is some constant chosen by hand, and E_{big} is some large energy. This means that V_{mod} is equal to E_{big} , when one of the distances d_i is zero, and very close to V , when none of the distances d_1, d_2, d_3 and d_4 are very small. In practice, we used

$$k = \left(\frac{1}{2a_0} \right)^4 \quad (13)$$

and

$$E_{\text{big}} = 10^9 \mu E_{\text{h}}. \quad (14)$$

We considered only geometries where the interaction energy did not exceed $100 \mu E_{\text{h}}$ leaving us with 6710 points, and fitted the adjustable parameters to the *ab initio* data. This gave us a good fit with an RMS deviation of $0.85 \mu E_{\text{h}}$ (0.2 cm^{-1}), indicating that the model is accurate in the region relevant to describing the bound states. Of course, ignoring the regions where the interaction energy is high, means that there is no reason to expect that the model performs well there. And indeed, computing the deviation from all the *ab initio* interaction energies gives us an RMSE of $31\,000 \mu E_{\text{h}}$.

The fitted value of the dimensionless dilation is $a = 4.3799$, and the rest of the parameters are given in Tab. II. From the first table entry, we see that $c_{(0,0,1,0)} = -32.12 \mu E_{\text{h}}$, so the first term in the sum giving V is

$$\begin{aligned} -32.12 \mu E_{\text{h}} T_{(0,0,1,0)} &= \frac{-32.12 \mu E_{\text{h}}}{2} (D_1^0 D_2^0 D_3^1 D_4^0 + D_1^0 D_2^0 D_3^0 D_4^1) \\ &= \frac{-32.12 \mu E_{\text{h}}}{2} (D_3 + D_4). \end{aligned} \quad (15)$$

Using the analytical expression for the IPES, we find the global minimum to be $-538.47 \mu E_{\text{h}}$ (-118.2 cm^{-1}), located at $r_0 = 7.856 a_0$, $\theta_1 = 111.34^\circ$, $\theta_2 = 159.70^\circ$, and $\phi_2 = 0^\circ$. A view of the IPES for $r_0 = 7.856 a_0$ and $\phi_2 = 0^\circ$ is depicted in Fig. 3. The minimal potential-energy configurations (all equal by symmetry) are marked with blue dots. A nearly barrierless disrotatory path permitting a floppy large-amplitude motion of the complex is observed. This result is similar to that found for the CO dimer [35].

The global minimum found in this work is by ca. 0.8 cm^{-1} deeper than those reported previously [18, 19]. The corresponding intermolecular distance is similar for all the three potentials (ca. $7.85\text{--}7.86 a_0$), while our θ_1 is slightly larger and θ_2 slightly smaller than those from previous studies [18, 19]. To further check the performance of the analytical fit, we evaluated some additional CCSD(T)/aug-cc-pVQZ-33211 interaction energies in the vicinity of the expected global minimum on a grid of points. The lowest interaction energy of -118.04 cm^{-1} was found at $r_0 = 7.8 a_0$, $\theta_1 = 109.0^\circ$, $\theta_2 = 162.0^\circ$, and $\phi_2 = 0^\circ$. This result is in concordance with that obtained from the fit.

IV. INTERMOLECULAR STATES

A. Variational calculations

The rovibrational levels of CO-N₂ were calculated using a variational method called DSL [36, 37] which uses a product basis with discrete variable representation (DVR) functions (D) [38] for the stretches and spherical harmonic type functions (S) for the bends and a symmetry adapted Lanczos eigensolver (L). The bend basis is appropriate for dealing with large amplitude bending motions. The calculation is carried out with the RV4 code [39] that implements the DSL method. It uses the polyspherical coordinates (r_1 , r_2 , r_0 , θ_1 , θ_2 , ϕ_2) associated with vector \mathbf{r}_1 (for CO), vector \mathbf{r}_2 (for N₂), and the Jacobi vector \mathbf{r}_0 , shown in Fig. 1. Because the intramonomer vibrational frequencies are much higher than their intermonomer counterparts, it is justified to fix r_1 and r_2 to their respective ground state values. In the DSL method, potential energy integrals are computed with Gauss quadrature. Eigenvalues and eigenvectors are determined with the symmetry-adapted Lanczos (SAL) algorithm [40, 41].

Since a thorough description of the DSL method applied to a similar system (N₂O)₂ is reported in Refs. 42, 43, only the computational details specific to the present study are given here. Each basis function is a product

$$f_{\alpha_0}(R)u_{l_1l_2m_2K}^{JMP}(\theta_1, \theta_2, \phi_2; \alpha, \beta, \gamma), \quad (16)$$

where $f_{\alpha_0}(R)$ is a DVR function for the stretch coordinate and $u_{l_1l_2m_2K}^{JMP}$ is the parity adapted bend-rotation function. The latter was expressed as a linear combination of two products of an associated Legendre function for θ_1 , a spherical harmonic function for (θ_2, ϕ_2) , and a Wigner function for the Euler angles (α, β, γ) , with $P = 0$ and $P = 1$ corresponding to even and odd parity, respectively.

In our calculation, we use the full permutation-inversion group of CO-N₂, G_4 . It has four irreducible representations: $A+$, $B+$, $A-$, and $B-$. A/B label levels that are symmetric/antisymmetric under permutation of the two N atoms. $+/-$ label even/odd levels. In our calculation, the levels of the two nuclear spin species are obtained in different symmetry blocks. CO-*ortho*N₂ levels appear in the A symmetry block and CO-*para*N₂ levels appear in the B symmetry block. The lowest level of CO-*ortho*N₂ is lower than the lowest level of CO-*para*N₂ because the two levels are associated with $j_{N_2} = 0$ and 1, respectively.

Because of the large-amplitude motion and the resulting low-lying vibrational states, rather than using a traditional asymmetric rotor Hamiltonian to fit the levels, spectroscopists group the rovibrational levels into stacks and fit the levels in each stack. A stack is labelled by $(j_{\text{CO}}, j_{\text{N}_2}; K, \sigma)$, where $\sigma = e/f$ corresponds to $(-1)^{J+P} = \pm 1$. Each stack of levels is fitted with a simple rotational energy level expression based on a linear rotor Hamiltonian with a doubling term that splits the e/f components of $K > 0$ stacks. See Eq. (1) of Ref. 2 for CO-N₂, which has been adopted in all subsequent CO-N₂ papers cited in this work. In our calculations, K can be unambiguously assigned by analysing the wavefunctions [35]. $j_{\text{CO}}, j_{\text{N}_2}$ are simply obtained by matching computed and experimental levels.

The parameters for computing the intermolecular rovibrational levels using the RV4 code are all given in Tab. III. The choice of the basis functions for r_0 merits further discussion. Usually a potential-optimized discrete variable representation (PODVR) basis [44, 45] is a good choice. The PODVR basis is efficient if a good reference potential, usually either a cut potential or a minimized potential, can be found. It has the advantage of being black-box because there are no parameters to adjust. For CO-N₂, bases obtained from the cut and minimized potentials are both poor, due to coupling. Owing to the fact that neither the cut nor the minimized PODVR basis is good, we use a tri-diagonal Morse (TDM) DVR basis [44]. However, it takes more effort to optimize the four parameters of the TDM DVR basis: D_e , ω_e , r_e and α . The first three parameters are optimized by comparing a few of the lowest $J = 0$ levels computed with a TDM basis and a set of benchmark levels computed using 120 sine DVR basis. Our final TDM DVR basis parameters are $D_e = 108 \text{ cm}^{-1}$, $\omega_e = 18 \text{ cm}^{-1}$, and $r_e = 8.45 a_0$. The fourth TDM DVR basis parameter α depends on the other parameters (α appears in the associated Laguerre polynomial L_n^α). As discussed in Ref. 46, we follow Wei and Carrington's choice [44], $\alpha = A - 2[A/2] = 0$ with $A = 4D_e/\omega_e = 24$ so that all the bound states of the Morse Hamiltonian are exactly reproduced by the TDM basis (the Morse Hamiltonian that corresponds to these parameters has $[A/2]=12$ bound states, fewer than the number of basis functions, $N_{r_0} = 30$).

B. Existing experimental data

We compare the experimental rovibrational levels on the $v_{\text{CO}} = 0$ ground state of the two spin species with our calculated levels. The experimental levels are collected from the

millimeter-wave (MMW) study by Surin *et al.* [8] and the IR study by Rezaei *et al.* [10]. There are 3 stacks of levels for CO-*ortho*N₂. They are, in the order of increasing energy, (0, 0, 0e), (1, 0, 1e/f), and (1, 0, 0e) and are labelled as stacks *a*, *b*, *c*. There are 5 stacks of levels for CO-*para*N₂. They are, in the order of increasing energy, (0, 1, 0e), (0, 1, 1e/f), (1, 1, 1e/f), (1, 1, 0e), and (1, 1, 2e/f) and are labelled as stacks *a*, *b*, *c*, *d*, *e* (see Tab. IV). Note that a correction term 0.0048 cm⁻¹ needs to be added to the (0, 1, 1f) levels of CO-*para*N₂ obtained from the MMW study (Tab. 8 of Ref. 8), which was first pointed out by Rezaei *et al.* in their IR study [10]. This is because the (0, 1, 1f) stack was not linked to other stacks in the MMW experiment and the band center of this stack was “floated” or corrected by Rezaei *et al.*. In the IR experiment of Rezaei *et al.* [10], the (0, 1, 1f) stack is linked with the (0, 1, 0e) stack *via* transitions to the common upper state (1, 1, 0e) of the $v_{\text{CO}} = 1$ excited state. We note that this correction is confirmed by a new MMW experiment [9] where the (0, 1, 1f) stack is again linked with the (0, 1, 0e) *via* transitions to the common upper state (0, 1, 0e).

C. Theoretical results

Even and odd levels for both CO-*ortho*N₂ and CO-*para*N₂ were computed for each J up to $J = 20$ and the complete set can be obtained from the authors on request. Levels up to $J = 10$ with experimental assignments are given in Tab. V for CO-*ortho*N₂. Levels up to $J = 8$ with experimental assignments are given in Tab. VI for CO-*para*N₂. A graphical comparison of the experimental and calculated intermolecular levels for CO-*ortho*N₂ and CO-*para*N₂ is presented in Figs. 4a and b, respectively. The agreement between theory and experiment is remarkably good, making assignments straightforward and unambiguous. They were also facilitated by knowing the symmetry of each of the computed levels, owing to the use of the symmetry adapted Lanczos procedure and by assigning K to each level using the wavefunctions.

Interestingly the agreement is significantly better for the CO-*ortho*N₂ levels, with an RMSE over 41 levels of just 0.017 cm⁻¹. Those errors are both positive and negative with an average close to zero. For the CO-*para*N₂ levels, the errors are larger (the RMSE for 40 levels is 0.045 cm⁻¹) and more systematic, as the computed levels are below the experimental ones in all cases. The level of agreement obtained in these results is among the best reported

in the literature for vdWs systems. It could be of interest to explore this further in terms of the hierarchy of electronic structure methods employed (also going beyond the CCSD(T) approximation). It remains to be determined whether various terms in high-level composite energies [47] for this system would be found to be negligible or if the currently adopted procedure benefits from particularly favourable cancellation of errors.

Variational calculations on *ab initio* IPESs seldom achieve accuracy as good as 1 cm^{-1} and accuracy better than 0.1 cm^{-1} is very rare. The lowest bending vibrational energy level has been observed for both spin species: 4.666 cm^{-1} for CO-*ortho*N₂ and 4.496 cm^{-1} for CO-*para*N₂. These two vibrational levels are linked by a red arrow in Fig. 4. For these two vibrational levels, the calculated minus observed differences are only 0.02 cm^{-1} and 0.07 cm^{-1} , respectively. It is rare to find this sort of accuracy for a vdW system. Much of the overall RMSE for the two spin species can be traced to the vibrational errors. Errors in differences between J levels for a particular stack are typically on the order of 0.001 cm^{-1} and never larger than 0.01 cm^{-1} (see e.g. Fig. 4). Errors in differences of rotational levels are smaller than for the corresponding vibrational levels for many molecules, because the structure of the molecule predicted by *ab initio* theory is usually more accurate than the shape of the IPES on which the vibrational levels depend.

The lowest two stacks, stack a ($K = 0$) and b ($K = 1$) of CO-*para*N₂ are closely spaced and strong Coriolis interaction between them was observed experimentally [5]. After analysing the wavefunctions, we have also found that some levels in these two stacks have two dominant K components. These levels are labelled as 01 or 10 in the K column of Tab. VI. 01 (10) means the $K = 0$ ($K = 1$) contribution is slightly larger than the $K = 1$ ($K = 0$) contribution (see Tab. VI). The same coupling was also discussed in the theoretical study of Surin *et al.* [19].

When compared to the results from the two most recent investigations [18, 19], our potential gives significantly better agreement with experimental data. In Ref. 18 the differences between the reported theoretical and the available experimental intermolecular energy levels are as large as 0.27 cm^{-1} , while in Ref. 19 these differences are considerably smaller. Here we further improve the results for the CO-N₂ complex, by evaluating a more accurate IPES, with the potential minimum close to the exact CCSD(T) result and with a better performance regarding the evaluation of the intermolecular states, lowering the RMSE from 0.1 to 0.038 cm^{-1} . This is clearly seen in Fig. 4 where the theoretical levels of Ref. 19 are

compared with our theoretical levels and the experimental levels.

V. SUMMARY AND CONCLUSIONS

An accurate IPES for the CO-N₂ dimer was constructed using the high-level *ab initio* CCSD(T)/aug-cc-pVQZ+33211 method. More than 10 000 calculated points were fitted to an analytical function. A symmetrized fitting approach yields an RMSE of 0.2 cm⁻¹ representing the data in the low energy regions relevant to the rovibrational levels computed in this study. Using the analytical fit of the IPES, we have found the global minimum with an energy of $-538.47 \mu E_h$ (-118.2 cm⁻¹) located at $r_0 = 7.856 a_0$, $\theta_1 = 111.34^\circ$, $\theta_2 = 159.70^\circ$, and $\phi_2 = 0^\circ$. The nominally T-shaped structures of the complex were confirmed, although a low-energy channel permitting floppy large-amplitude motion was observed.

The symmetry-adapted Lanczos method was used in highly converged rovibrational variational calculations. Stacks of rovibrational levels for both CO-*ortho*N₂ and CO-*para*N₂ were computed up to $J = 20$. The accuracy of the IPES is remarkable, with an RMSE of only 0.038 cm⁻¹ over 81 experimentally assigned levels. This new potential considerably improves those previously evaluated for the complex, in particular the most accurate available [19], providing exceptionally good agreement between the calculated and the experimental intermolecular states.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgments

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FIG. 1: The intermolecular coordinates r_0, θ_1, θ_2 and ϕ_2

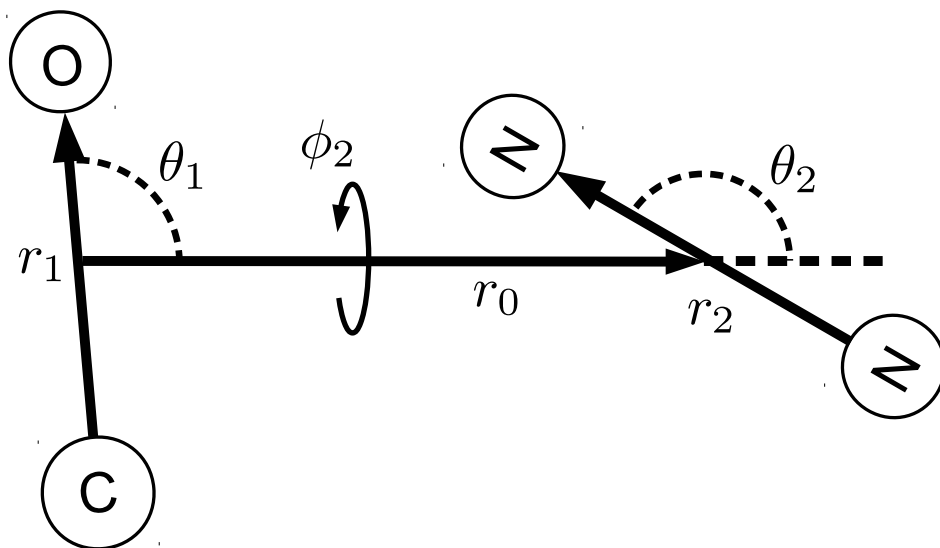


FIG. 2: A slice of the CO-N₂ IPES for $r_0 = 3.70426 \text{ \AA}$ ($7.0 a_0$), $\theta_1 = 90^\circ$, and $\phi_2 = 0.0^\circ$ reproduced with the Gauss-Lobatto interpolations for $n = 10, \dots, 16$. The exact interaction energy values at the Gauss-Lobatto points are marked with black circles; some additional energies are marked with red squares. Two zoomed areas are presented in inner graphs a) and b) (see text for more details)

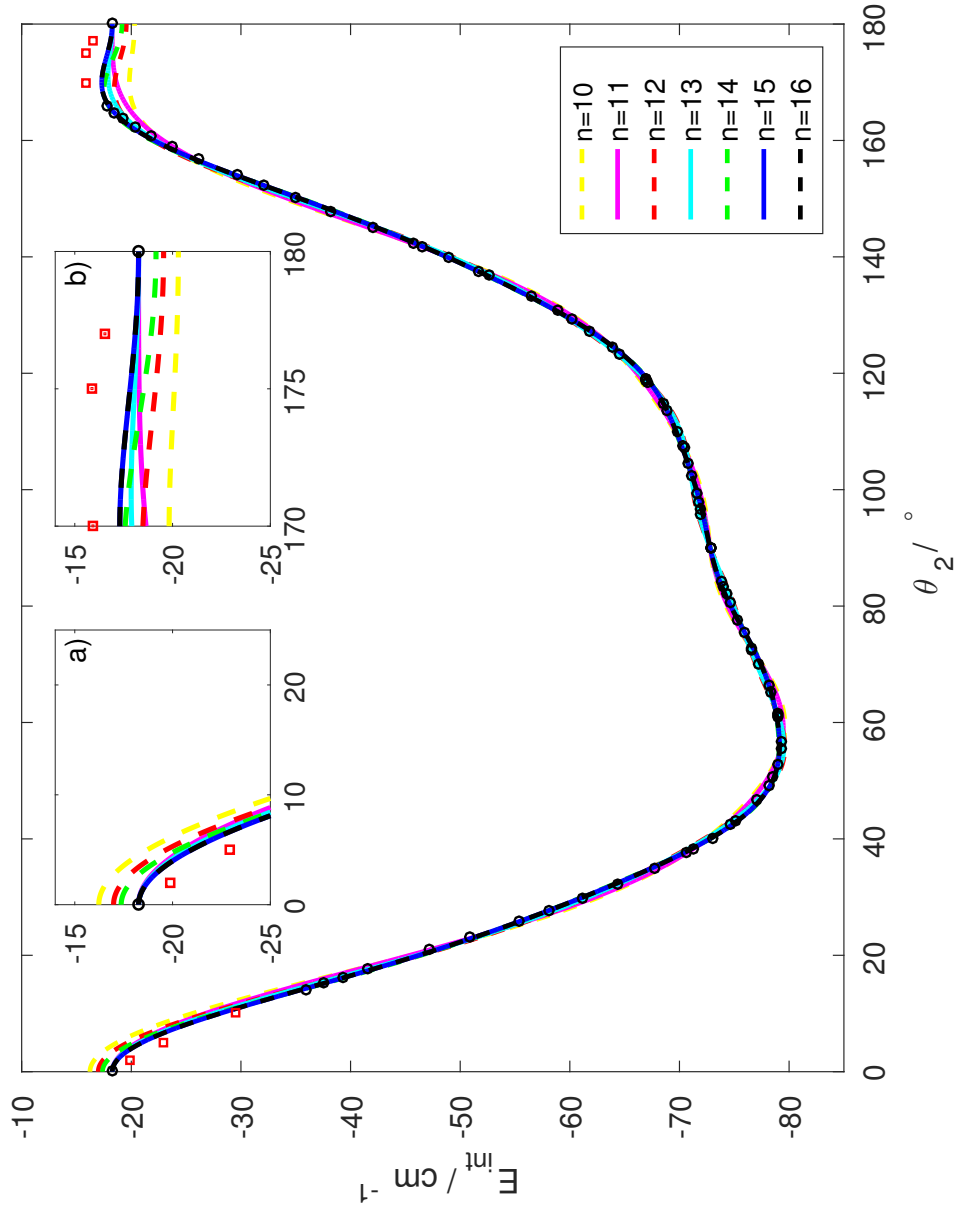


FIG. 3: CO-N₂ IPES for $r_0 = 7.856 a_0$ and $\phi_2 = 0^\circ$. The minimal potential energy configuration is marked with blue dots

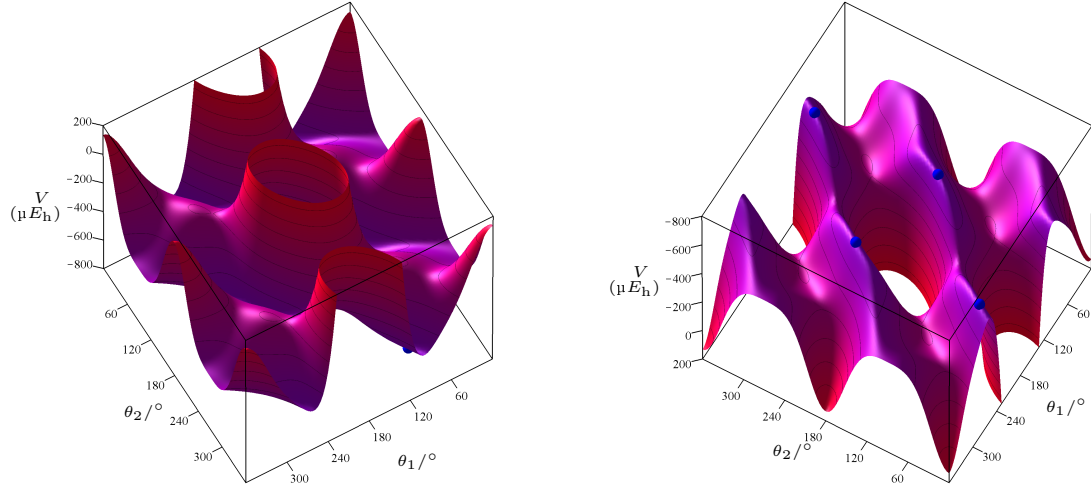


FIG. 4: A comparison of experimental (red) and calculated (black) intermolecular levels for CO-*ortho*N₂ in panel (a) and CO-*para*N₂ in panel (b). Two sets of calculated levels are given: from this study and from Ref. 19 (italics). For each stack labelled by K , levels are given for $J = K, K + 1, \dots$ from the bottom up and the maximum J is 2. The zero of panel (b) for the calculated levels is at 2.7365 cm^{-1} relative to the scale of panel (a)

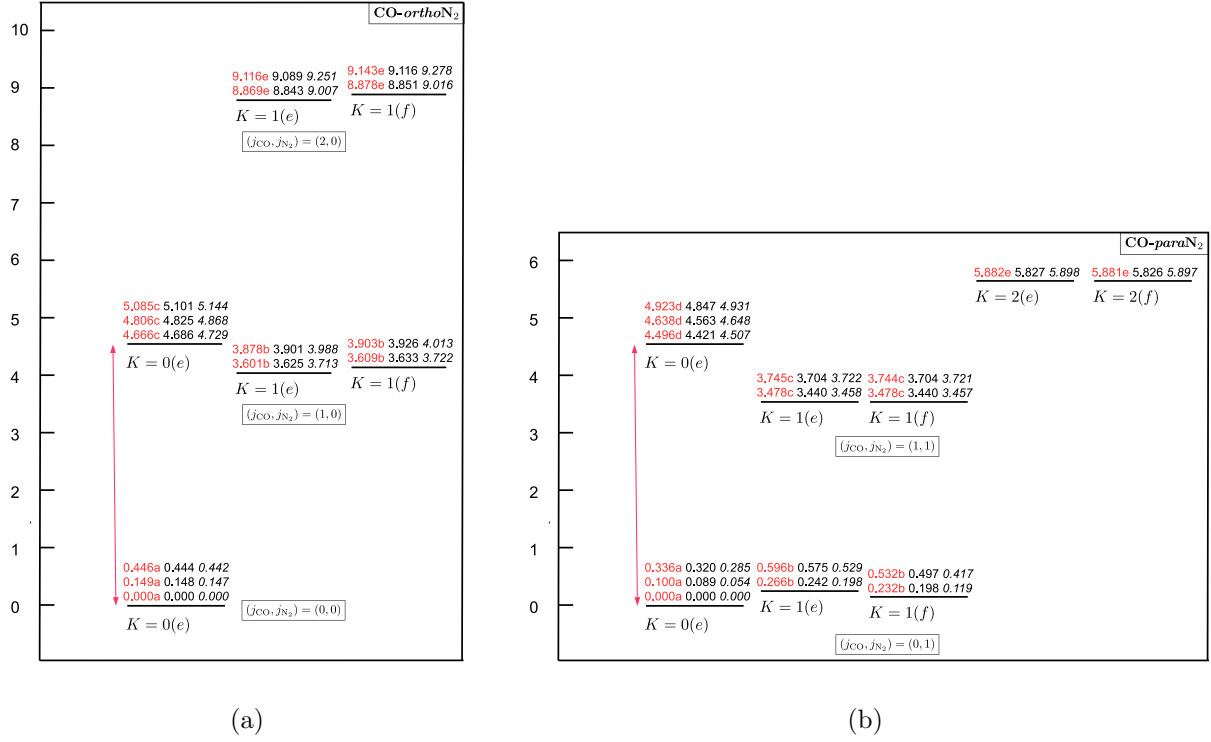


TABLE I: Interaction energies (in cm^{-1}) calculated at the CCSD(T) level for $r_0 = 4.498 \text{ \AA}$, $\theta_1 = \theta_2$, and $\phi_2 = 0.0^\circ$. "mb" stands for the 33211 midbond set, "un" for a fully uncontracted basis set, and "rel" for the relativistic calculations using the second order Douglas-Kroll-Hess Hamiltonian (*cf.* text for details)

$\theta_1 = \theta_2$	Frozen core						All electron				
	aDZ	aTZ	aQZ	a5Z	aTZ+mb	aQZ+mb	daTZ+mb	un-aTZ+mb	un-aTZ+mb	aCTZ+mb	aCTZ+mb-rel
0	226.71	195.43	184.34	180.44	182.63	179.52	182.93	182.77	181.79	181.74	181.76
15	117.36	91.50	81.98	78.57	79.23	77.44	79.53	79.83	80.38	79.07	79.09
30	-43.46	-58.69	-64.63	-66.91	-68.41	-68.45	-68.42	-67.55	-67.31	-67.91	-67.90
45	-89.11	-97.25	-100.08	-101.41	-103.78	-102.98	-104.03	-103.03	-103.09	-103.18	-103.19
60	-63.00	-68.65	-70.05	-70.85	-72.91	-72.09	-73.26	-72.39	-72.41	-72.44	-72.44
75	-35.87	-41.14	-42.21	-42.73	-44.18	-43.63	-44.48	-43.86	-43.83	-43.81	-43.81
90	-28.34	-33.45	-34.61	-35.03	-36.06	-35.72	-36.27	-35.79	-35.73	-35.70	-35.70
105	-37.07	-42.01	-43.36	-43.79	-44.65	-44.46	-44.88	-44.41	-44.34	-44.33	-44.33
120	-52.81	-57.89	-59.30	-59.81	-60.96	-60.62	-61.16	-60.59	-60.53	-60.56	-60.57
135	-63.46	-69.61	-70.98	-71.62	-73.39	-72.64	-73.49	-72.78	-72.75	-72.84	-72.84
150	-56.41	-64.97	-66.63	-67.38	-69.72	-68.57	-69.67	-68.90	-68.94	-69.03	-69.03
165	-31.40	-42.74	-45.13	-46.00	-48.65	-47.31	-48.27	-47.66	-47.78	-47.85	-47.84
180	-15.72	-28.25	-31.08	-32.05	-34.75	-33.41	-34.18	-33.68	-33.84	-33.90	-33.88

TABLE II: Parameters of the fit V . We write $e_1e_2e_3e_4$ as an abbreviation for (e_1, e_2, e_3, e_4) , e.g. $(0, 0, 1, 0)$ simply becomes 0010

\mathbf{e}	$c_{\mathbf{e}}/\mu E_h$	\mathbf{e}	$c_{\mathbf{e}}/\mu E_h$	\mathbf{e}	$c_{\mathbf{e}}/\mu E_h$
0010	-32.12	0020	42 713.23	0101	-90 922.33
2000	45 622.21	0011	-43 921.71	0110	94 044.83
1100	-47 238.94	0003	-94 238.97	1020	222 526.29
0201	-151 150.54	3000	23 820.70	0012	99 515.71
1011	-151 182.26	0210	49 958.19	0120	-87 836.88
1110	113 802.42	1200	-27 029.72	0040	134 244.43
0103	-261 135.27	2020	270 883.97	0301	-309 531.19
4000	161 306.19	0031	-143 021.61	0112	-57 524.72
2011	27 878.69	3001	179 528.32	0121	344 483.45
2002	-226 068.08	1201	553 579.66	3100	-534 808.10
1111	-86 760.14	2101	-427 291.73	2200	377 662.86
0050	-38 254.79	0302	128 635.65	0401	-68 503.93
5000	-26 919.29	0014	-28 092.38	1031	332 771.36
0212	-243 575.99	3011	-56 721.87	0023	69 469.78
1022	-339 359.60	2012	346 112.63	0320	-93 145.80
2003	-33 678.04	1130	114 684.93	1202	-583 925.14
3110	469 398.51	1112	-189 641.53	2111	124 011.68
1310	86 557.42	2102	486 416.22	2201	-480 243.41
3200	20 583.83	0006	12 990.26	0105	-12 025.49
2040	6503.89	0501	-27 982.02	6000	27 639.18
0015	-12 989.92	2031	-62 247.86	0312	56 617.25
5001	6922.38	2022	92 503.82	0321	-76 139.61
4002	-4820.57	1023	-8329.71	0231	-75 468.23
3003	30 006.87	0141	20 848.49	1140	-7453.07
1203	34 335.28	4110	18 736.81	1500	-59 868.76
1122	44 846.43	1230	-38 456.68	2400	57 833.68
3300	-22 747.36				

TABLE III: Parameters for CO-N₂. For TDM DVR parameters see Refs. 46 and 44

$B_0(\text{CO}) = 1.9225125 \text{ cm}^{-1}$ [48]
$B_0(\text{N}_2) = 1.98950 \text{ cm}^{-1}$ [49]
$m_{(\text{N})} = 14.0030740052$
$m_{(\text{O})} = 15.9949146221$
$r_0(\text{CO}) = 2.13201 a_0$ [25]
$r_0(\text{N}_2) = 2.07397 a_0$ [25]
$l_{1x} = l_{2x} = m_{2x} = 37$
$N_{\theta_1} = N_{\theta_2} = 38, N_{\phi_2} = 80$
DVR parameters
$D_e = 108 \text{ cm}^{-1}, \omega_e = 18 \text{ cm}^{-1}, r_0^e = 8.45a_0, \alpha = A - 2[A/2] = 0$
$N_{r_0} = 30$
$N_{bas} = 279870$ (even parity and even l_2 for CO- <i>ortho</i> N ₂)
$V_{\text{ceil}} = 2098.4 \text{ cm}^{-1}$.

TABLE IV: Stack labels for the CO-*ortho*N₂ and CO-*para*N₂ observed $v_{\text{CO}} = 0$ states. The stacks are labelled in the order of increasing energy. The order of stacks for CO-*ortho*N₂ follow that of the $v_{\text{CO}} = 1$ state [10] because more stacks are observed.

CO- <i>ortho</i> N ₂	label	$(j_{\text{CO}}, j_{\text{N}_2}, K, e/f)$	Ref.
	a	(0, 0, 0e)	8
	b	(1, 0, 1e/f)	8
	c	(1, 0, 0e)	8
	d	(2, 0, 2e/f)	
	e	(2, 0, 1e/f)	19
	f	(2, 0, 0e/f)	
	g	(1, 2, 0e)	
	h	(1, 2, 1e/f)	
CO- <i>para</i> N ₂	label	$(j_{\text{CO}}, j_{\text{N}_2}, K, e/f)$	
	a	(0, 1, 0e)	8
	b	(0, 1, 1e/f)	8
	c	(1, 1, 1e/f)	8
	d	(1, 1, 0e)	10, 19
	e	(1, 1, 2e/f)	10, 19

TABLE V: Comparison between the theoretical and the experimental $J \leq 10$ energy levels of CO-*ortho*N₂ (in cm⁻¹). Stack labels are defined in Tab. IV. All levels are relative to the ZPE of CO-*ortho*N₂ -76.1252 cm⁻¹. PI group symmetry and spectroscopy parity e/f are also indicated.

$J = 0, A^+(e)$				$J = 0, A^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.0000	0.0000	0	<i>a</i>	16.0601		0	
4.6863	4.6663	0	<i>c</i>	23.7748		0	
$J = 1, A^+(f)$				$J = 1, A^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
3.6333	3.6093	1	<i>b</i>	0.1480	0.1486	0	<i>a</i>
8.8514	8.8780	1	<i>e</i>	3.6249	3.6009	1	<i>b</i>
13.5885		1		4.8246	4.8057	0	<i>c</i>
15.4695		1		8.8425	8.8691	1	<i>e</i>
$J = 2, A^+(e)$				$J = 2, A^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.4439	0.4457	0	<i>a</i>	3.9262	3.9034	1	<i>b</i>
3.9010	3.8781	1	<i>b</i>	9.1155	9.1425	1	<i>e</i>
5.1013	5.0845	0	<i>c</i>	9.9916		2	
9.0893	9.1161	1	<i>e</i>	11.3735		2	
$J = 3, A^+(f)$				$J = 3, A^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
4.3652	4.3441	1	<i>b</i>	0.8875	0.8910	0	<i>a</i>
9.5128	9.5402	1	<i>e</i>	4.3146	4.2934	1	<i>b</i>
10.4358		2		5.5162	5.5026	0	<i>c</i>
11.8065		2		9.4616	9.4890	1	<i>e</i>
$J = 4, A^+(e)$				$J = 4, A^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack

1.4785	1.4843	0	<i>a</i>	4.9497	4.9310	1	<i>b</i>
4.8652	4.8464	1	<i>b</i>	10.0439	10.0725	1	<i>e</i>
6.0693	6.0600	0	<i>c</i>	11.0262		2	
9.9611	9.9896	1	<i>e</i>	12.3833		2	
$J = 5, A^+(f)$				$J = 5, A^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
5.6792	5.6634	1	<i>b</i>	2.2163	2.2250	0	<i>a</i>
10.7099	10.7403	1	<i>e</i>	5.5519	5.5363	1	<i>b</i>
11.7615		2		6.7606	6.7565	0	<i>c</i>
13.1033		2		10.5890	10.6200	1	<i>e</i>
$J = 6, A^+(e)$				$J = 6, A^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
3.1003	3.1127	0	<i>a</i>	6.5527	6.5406	1	<i>b</i>
6.3738	6.3623	1	<i>b</i>	11.5114	11.5446	1	<i>e</i>
7.5900	7.5921	0	<i>c</i>	12.6406		2	
11.3467	11.3808	1	<i>e</i>	13.9657		2	
$J = 7, A^+(f)$				$J = 7, A^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
7.5694	7.5616	1	<i>b</i>	4.1300	4.1466	0	<i>a</i>
12.4489	12.4862	1	<i>e</i>	7.3298	7.3234	1	<i>b</i>
13.6627		2		8.5574	8.5664	0	<i>c</i>
14.9699		2		12.2348	12.2715	1	<i>e</i>
$J = 8, A^+(e)$				$J = 8, A^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
5.3043	5.3257	0	<i>a</i>	8.7279	8.7250	1	<i>b</i>
8.4187	8.4184	1	<i>b</i>	13.5227	13.5652	1	<i>e</i>
9.6626	9.6795	0	<i>c</i>	14.8269		2	
13.2537	13.2885	1	<i>e</i>	16.1147		2	
$J = 9, A^+(f)$				$J = 9, A^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack

10.0270	10.0294	1	<i>b</i>	6.6222	6.6488	0	<i>a</i>
14.7331		1		9.6391	9.6461	1	<i>b</i>
16.1324		2		10.9052	10.9311	0	<i>c</i>
$J = 10, A^+(e)$				$J = 10, A^-(f)$			
cal.	obs.	K stack		cal.	obs.	K stack	
8.0825	8.1140	0	<i>a</i>	11.4650	11.4725	1	<i>a</i>
10.9897	11.0050	1	<i>b</i>	16.0800		1	
12.2848	12.3208	0	<i>c</i>	17.5785		2	

TABLE VI: Comparison between the theoretical and the experimental $J \leq 8$ energy levels of CO-*para*N₂ (in cm⁻¹). Stack labels are defined in Tab. IV. The ZPE of CO-*para*N₂ is 2.7365 cm⁻¹ higher than that of CO-*ortho*N₂. PI group symmetry and spectroscopy parity e/f are also indicated.

$J = 0, B^+(e)$				$J = 0, B^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.0000	0.0000	0	<i>a</i>	6.4110		0	
4.4205	4.4955	0	<i>d</i>	15.1054		0	
$J = 1, B^+(f)$				$J = 1, B^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.1979	0.2324	1	<i>b</i>	0.0887	0.1002	01	<i>a</i>
3.4397	3.4781	1	<i>c</i>	0.2420	0.2655	10	<i>b</i>
6.5472		0		3.4398	3.4784	1	<i>c</i>
7.4532		1		4.5625	4.6382	0	<i>d</i>
$J = 2, B^+(e)$				$J = 2, B^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.3200	0.3360	01	<i>a</i>	0.4970	0.5324	1	<i>b</i>
0.5751	0.5962	10	<i>b</i>	3.7040	3.7445	1	<i>c</i>
3.7043	3.7453	1	<i>c</i>	5.8264	5.8816	2	<i>e</i>
4.8465	4.9234	0	<i>d</i>	6.8191		0	
5.8265	5.8818	2	<i>e</i>	7.7598		1	
$J = 3, B^+(f)$				$J = 3, B^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
0.9453	0.9822	1	<i>b</i>	0.6932	0.7128	0	<i>a</i>
4.1011	4.1445	1	<i>c</i>	1.0476	1.0684	1	<i>b</i>
6.2848	6.3405	2	<i>e</i>	4.1016	4.1461	1	<i>c</i>
7.2258		0		5.2724	5.3510	0	<i>d</i>
8.2201		1		6.2854	6.3411	2	<i>e</i>

$J = 4, B^+(e)$				$J = 4, B^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
1.2080	1.2313	0	a	1.5426	1.5813	1	b
1.6588	1.6803	1	b	4.6314	4.6789	1	c
4.6320	4.6812	1	c	6.8943	6.9509	2	e
5.8397	5.9208	0	d	7.7662		0	
6.8961	6.9526	2	e	8.8340		1	
$J = 5, B^+(f)$				$J = 5, B^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
2.2883	2.3295	1	b	1.8644	1.8916	0	a
5.2955	5.3481	1	c	2.4074	2.4305	1	b
7.6535	7.7114	2	e	5.2962	5.3511	1	c
8.4395		0		6.5482	6.6324	0	d
9.6013		1		7.6578	7.7155	2	e
$J = 6, B^+(e)$				$J = 6, B^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
2.6618	2.6935	0	a	3.1818	3.2259	1	b
3.2924	3.3177	1	b	6.0942	6.1527	1	c
6.0945	6.1562	1	c	8.5608	8.6204	2	e
7.3975	7.4855	0	d	9.2448		0	
8.5695	8.6288	2	e	10.5216		1	
$J = 7, B^+(f)$				$J = 7, B^-(e)$			
cal.	obs.	K	stack	cal.	obs.	K	stack
4.2224	4.2701	1	b	3.5997	3.6365	0	a
7.0277	7.0933	1	c	4.3121	4.3406	1	b
9.6134	9.6758	2	e	7.0274	7.0969	1	c
10.1823		0		8.3872	8.4797	0	d
11.5940		1		9.6302	9.6915	2	e
$J = 8, B^+(e)$				$J = 8, B^-(f)$			
cal.	obs.	K	stack	cal.	obs.	K	stack

4.6774	4.7199	0	<i>a</i>	5.4090	5.4609	1	<i>b</i>
5.4652	5.4976	1	<i>b</i>	8.0966	8.1703	1	<i>c</i>
8.0951	8.1734	1	<i>c</i>	10.8068	10.8743	2	<i>e</i>
9.5167	9.6145	0	<i>d</i>	11.2540		1	
10.8387	10.9021	2	<i>e</i>	12.8170		1	

The table of contents entry: We present a highly accurate *ab initio* intermolecular potential-energy surface and rovibrational spectrum for the CO-N₂ complex.

